## CHAPTER 13

## **Query Processing**

## **Solutions to Practice Exercises**

**13.1** Query:

$$\Pi_{T.branch\_name}((\Pi_{branch\_name,\ assets}(\rho_T(branch))) \bowtie_{T.assets>S.assets} (\Pi_{assets}(\sigma_{(branch\_city='Brooklyn')}(\rho_S(branch)))))$$

This expression performs the theta join on the smallest amount of data possible. It does this by restricting the right hand side operand of the join to only those branches in Brooklyn, and also eliminating the unneeded attributes from both the operands.

**13.2** We will refer to the tuples (kangaroo, 17) through (baboon, 12) using tuple numbers  $t_1$  through  $t_{12}$ . We refer to the  $j^{th}$  run used by the  $i^{th}$  pass, as  $r_{ij}$ . The initial sorted runs have three blocks each. They are:

$$\begin{array}{rcl} r_{11} & = & \{t_3, t_1, t_2\} \\ r_{12} & = & \{t_6, t_5, t_4\} \\ r_{13} & = & \{t_9, t_7, t_8\} \\ r_{14} & = & \{t_{12}, t_{11}, t_{10}\} \end{array}$$

Each pass merges three runs. Therefore the runs after the end of the first pass are:

$$r_{21} = \{t_3, t_1, t_6, t_9, t_5, t_2, t_7, t_4, t_8\}$$
  
 $r_{22} = \{t_{12}, t_{11}, t_{10}\}$ 

At the end of the second pass, the tuples are completely sorted into one run:

$$r_{31} = \{t_{12}, t_3, t_{11}, t_{10}, t_1, t_6, t_9, t_5, t_2, t_7, t_4, t_8\}$$

- 13.3  $r_1$  needs 800 blocks, and  $r_2$  needs 1500 blocks. Let us assume M pages of memory. If M>800, the join can easily be done in 1500 + 800 disk accesses, using even plain nested-loop join. So we consider only the case where  $M\leq 800$  pages.
  - **a.** Nested-loop join:

Using  $r_1$  as the outer relation we need 20000\*1500+800 = 30,000,800 disk accesses, if  $r_2$  is the outer relation we need 45000\*800 + 1500 = 36,001,500 disk accesses.

**b.** Block nested-loop join:

If  $r_1$  is the outer relation, we need  $\lceil \frac{800}{M-1} \rceil * 1500 + 800$  disk accesses, if  $r_2$  is the outer relation we need  $\lceil \frac{1500}{M-1} \rceil * 800 + 1500$  disk accesses.

**c.** Merge-join:

Assuming that  $r_1$  and  $r_2$  are not initially sorted on the join key, the total sorting cost inclusive of the output is  $B_s = 1500(2\lceil log_{M-1}(1500/M)\rceil + 2) + 800(2\lceil log_{M-1}(800/M)\rceil + 2)$  disk accesses. Assuming all tuples with the same value for the join attributes fit in memory, the total cost is  $B_s + 1500 + 800$  disk accesses.

d. Hash-join:

We assume no overflow occurs. Since  $r_1$  is smaller, we use it as the build relation and  $r_2$  as the probe relation. If M > 800/M, i.e. no need for recursive partitioning, then the cost is 3(1500 + 800) = 6900 disk accesses, else the cost is  $2(1500 + 800) \lceil log_{M-1}(800) - 1 \rceil + 1500 + 800$  disk accesses.

13.4 If there are multiple tuples in the inner relation with the same value for the join attributes, we may have to access that many blocks of the inner relation for each tuple of the outer relation. That is why it is inefficient. To reduce this cost we can perform a join of the outer relation tuples with just the secondary index leaf entries, postponing the inner relation tuple retrieval. The result file obtained is then sorted on the inner relation addresses, allowing an efficient physical order scan to complete the join.

Hybrid merge–join requires the outer relation to be sorted. The above algorithm does not have this requirement, but for each tuple in the outer relation it needs to perform an index lookup on the inner relation. If the outer relation is much larger than the inner relation, this index lookup cost will be less than the sorting cost, thus this algorithm will be more efficient.

13.5 We can store the entire smaller relation in memory, read the larger relation block by block and perform nested loop join using the larger one as the outer relation. The number of I/O operations is equal to  $b_r + b_s$ , and memory requirement is  $min(b_r, b_s) + 2$  pages.

- **13.6 a.** Use the index to locate the first tuple whose *branch\_city* field has value "Brooklyn". From this tuple, follow the pointer chains till the end, retrieving all the tuples.
  - **b.** For this query, the index serves no purpose. We can scan the file sequentially and select all tuples whose *branch\_city* field is anything other than "Brooklyn".
  - c. This query is equivalent to the query

```
\sigma_{(branch\_city \ge 'Brooklyn' \land assets < 5000)}(branch)
```

Using the *branch-city* index, we can retrieve all tuples with *branch-city* value greater than or equal to "Brooklyn" by following the pointer chains from the first "Brooklyn" tuple. We also apply the additional criteria of assets < 5000 on every tuple.

13.7 Let *outer* be the iterator which returns successive tuples from the pipelined outer relation. Let *inner* be the iterator which returns successive tuples of the inner relation having a given value at the join attributes. The *inner* iterator returns these tuples by performing an index lookup. The functions IndexedNLJoin::open, IndexedNLJoin::close and IndexedNLJoin::next to implement the indexed nested-loop join iterator are given below. The two iterators *outer* and *inner*, the value of the last read outer relation tuple t<sub>r</sub> and a flag *done<sub>r</sub>* indicating whether the end of the outer relation scan has been reached are the state information which need to be remembered by IndexedNLJoin between calls.

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IndexedNLJoin::close()
begin
    outer.close();
    inner.close();
end
```

```
boolean IndexedNLJoin::next()
begin
     while(\neg done_r)
    begin
          if(inner.next(t_r[JoinAttrs]) \neq false)
          begin
               move tuple from inner's output buffer to t_s;
               compute t_r \bowtie t_s and place it in output buffer;
               return true;
          end
          else
               if(outer.next() \neq false)
               begin
                    move tuple from outer's output buffer to t_r;
                    rewind inner to first tuple of s;
               end
               else
                    done_r := true;
     end
     return false;
end
```

**13.8** Suppose  $r(T \cup S)$  and s(S) be two relations and  $r \div s$  has to be computed.

For sorting based algorithm, sort relation s on S. Sort relation r on (T,S). Now, start scanning r and look at the T attribute values of the first tuple. Scan r till tuples have same value of T. Also scan s simultaneously and check whether every tuple of s also occurs as the S attribute of r, in a fashion similar to merge join. If this is the case, output that value of T and proceed with the next value of T. Relation s may have to be scanned multiple times but r will only be scanned once. Total disk accesses, after sorting both the relations, will be |r| + N \* |s|, where N is the number of distinct values of T in r.

We assume that for any value of T, all tuples in r with that T value fit in memory, and consider the general case at the end. Partition the relation r on attributes in T such that each partition fits in memory (always possible because of our assumption). Consider partitions one at a time. Build a hash table on the tuples, at the same time collecting all distinct T values in a separate hash table. For each value of T, Now, for each value  $V_T$  of T, each value S of S, probe the hash table on S0. If any of the values is absent, discard the value S1 else output the value S2.

In the case that not all r tuples with one value for T fit in memory, partition r and s on the S attributes such that the condition is satisfied, run the algorithm on each corresponding pair of partitions  $r_i$  and  $s_i$ . Output the intersection of the T values generated in each partition.

**13.9** Seek overhead is reduced, but the the number of runs that can be merged in a pass decreases potentially leading to more passes Should choose a value of  $b_b$  that minimizes overall cost.